

Unit-I : Set Theory & Logic

- **Introduction:** Variables, The Language of Sets, The Language of Relations and Function
- **Set Theory:** Definitions and the Element Method of Proof, Properties of Sets, Disproof, Algebraic Proofs, Boolean Algebras, **Russell's Paradox and the Halting Problem.**
- **The Logic of Compound Statements:** Logical Form and Logical Equivalence, Conditional Statements, Valid and Invalid Arguments.

Unit-II : Quantifiers & Number Theory

- **Quantified Statements:** Predicates and Quantified Statements, Statements with Multiple Quantifiers, Arguments with Quantified Statements
- **Elementary Number Theory and Methods of Proof:** Introduction to Direct Proofs, Rational Numbers, Divisibility, Division into Cases and the Quotient-Remainder Theorem, Floor and Ceiling, Indirect Argument: Contradiction and Contraposition, Two Classical Theorems, Applications in algorithms.

Unit-III : Sequences, Mathematical Induction, and Recursion

- **Sequences, Mathematical Induction,** Strong Mathematical Induction and the Well Ordering Principle for the Integers, Correctness of algorithms,
- Defining **sequences recursively**, solving recurrence relations by iteration, Second order linear homogenous recurrence relations with constant coefficients. General Recursive definitions and structural induction.
- **Functions:** Functions Defined on General Sets, One-to-One and Onto, Inverse Functions, Composition of Functions, Cardinality with Applications to Computability

Unit-IV: Relation & Graph Theory and Tree

- **Relations:** Relations on Sets, Reflexivity, Symmetry, and Transitivity, Equivalence Relations, Partial Order Relations
- **Graphs and Trees:** Definitions and Basic Properties, Trails, Paths, and Circuits, Matrix Representations of Graphs, Isomorphism's of Graphs, Trees, Rooted Trees, Spanning trees and shortest paths.

Unit-V : Counting and Probability

- **Introduction,** Possibility Trees and the Multiplication Rule,
- **Counting Elements of Disjoint Sets:** The Addition Rule, **The Pigeonhole Principle,**
- **Counting Subsets of a Set:** Combinations, r Combinations with Repetition Allowed, Probability Axioms and Expected Value, Conditional Probability, Bayes' Formula, and Independent Events.

List of Practical: Write the programs for the following using SCILAB

1. Set Theory

- a) Inclusion Exclusion principle.
- b) Power Sets
- c) Mathematical Induction

2. Functions and Algorithms

- a) Recursively defined functions
- b) Cardinality
- c) Polynomial evaluation
- d) Greatest Common Divisor

3. Counting

- a) Sum rule principle
- b) Product rule principle
- c) Factorial
- d) Binomial coefficients
- e) Permutations
- f) Permutations with repetitions
- g) Combinations
- h) Combinations with repetitions
- i) Ordered partitions
- j) Unordered partitions

4. Probability Theory

- a) Sample space and events
- b) Finite probability spaces
- c) Equiprobable spaces
- d) Addition Principle
- e) Conditional Probability
- f) Multiplication theorem for conditional probability
- g) Independent events
- h) Repeated trials with two outcomes

5. Graph Theory

- a) Paths and connectivity
- b) Minimum spanning tree
- c) Isomorphism

6. Directed Graphs

- a) Adjacency matrix
- b) Path matrix

7. Properties of integers

- a) Division algorithm
- b) Primes
- c) Euclidean algorithm
- d) Fundamental theorem of arithmetic
- e) Congruence relation
- f) Linear congruence equation

8. Algebraic Systems

- a) Properties of operations
- b) Roots of polynomials

9. Boolean Algebra

- a) Basic definitions in Boolean Algebra
- b) Boolean algebra as lattices

10. Recurrence relations

- a) Linear homogeneous recurrence relations with constant coefficients
- b) Solving linear homogeneous recurrence relations with constant coefficients
- c) Solving general homogeneous linear recurrence relations